## Problem Set 7 Introduction to Modal Logic Institute for Logic, Language and Computation Universiteit van Amsterdam

## Due November 18, 2005

- 1. 3.6.1 (a)
- 2. Suppose that  $\Gamma$  is a  $\Lambda$ -MCS. Prove the following two facts:
  - (a)  $\Lambda \subseteq \Gamma$ ; and
  - (b) For any two formulas  $\phi$  and  $\psi$ ,  $\phi \lor \psi \in \Gamma$  iff either  $\phi \in \Gamma$  or  $\psi \in \Gamma$ .
- 3. Complete the proof of Lindenbaum's Lemma. That is, if  $\Delta$  is the set of formulas constructed in the proof, prove that  $\Delta$  is a  $\Lambda$ -MCS.