



Robust Haptic Teleoperation of a Mobile Manipulation Platform

Jaeheung Park, Oussama Khatib

Stanford AI Lab, Stanford University

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

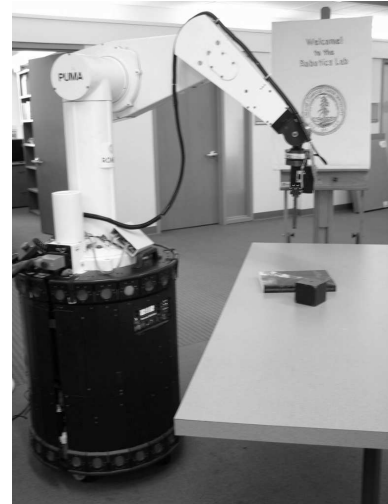
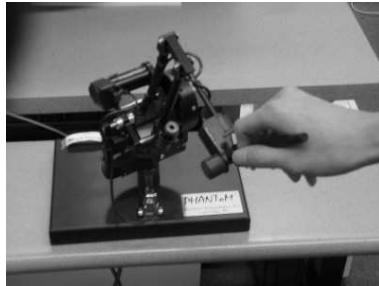
Experimental Results

Conclusion

Juliet Setting a Dinner...



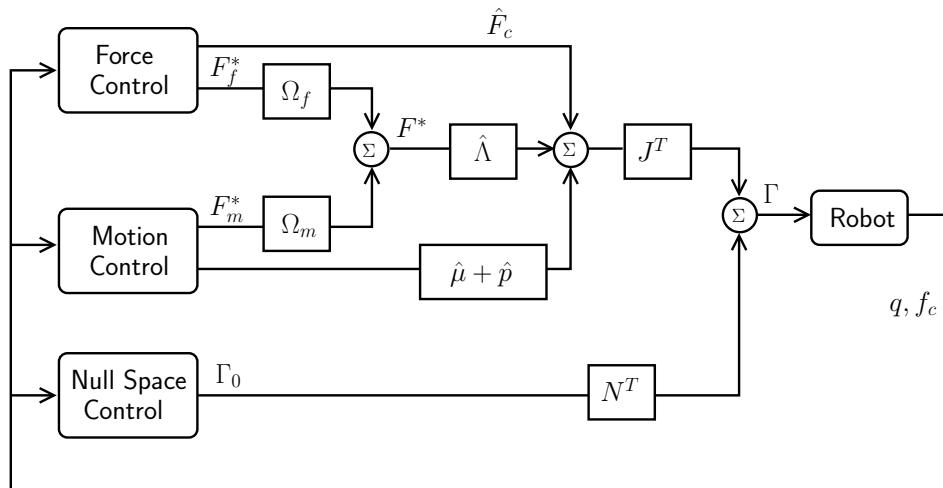
1. System Setup



- Master Haptic Device: PHANTOM 1.0 SensAble
- Slave Mobile Manipulator: PUMA560 on XR4000

<i>System Setup</i>
<i>Control of a Mobile...</i>
<i>Teleoperation</i>
<i>Force Control</i>
<i>Stiffness Estimation</i>
<i>Experimental Results</i>
<i>Conclusion</i>
<i>Juliet Setting a Dinner...</i>

2. Control of a Mobile Manipulator



The equations of motion for the end-effector:

$$\Lambda(q)\dot{v} + \mu(q, \dot{q}) + p(q) + F_c = F$$

Control:

$$\Gamma = J^T F + N^T \Gamma_0$$

$$F = \hat{\Lambda} F^* + \hat{\mu} + \hat{p} + \hat{F}_c$$

where $F^* = \Omega_f F_f^* + \Omega_m F_m^*$

System Setup

Control of a Mobile...

Teleoperation

Force Control

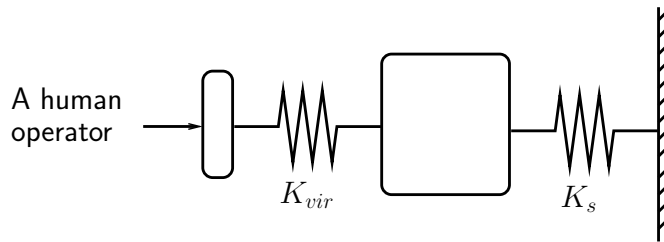
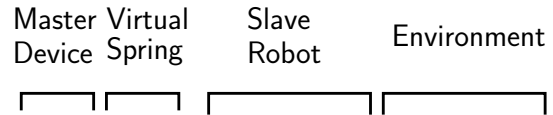
Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...

3. Teleoperation



System Setup

Control of a Mobile...

Teleoperation

Force Control

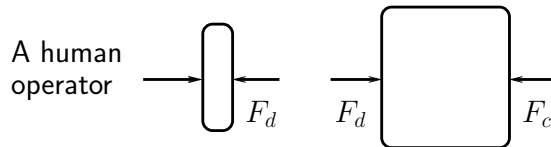
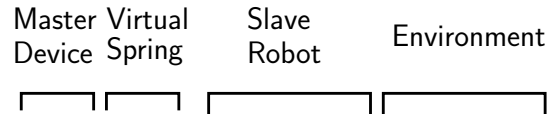
Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...

3. Teleoperation



System Setup

Control of a Mobile...

Teleoperation

Force Control

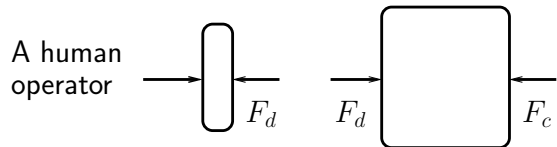
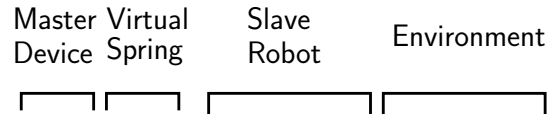
Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...

3. Teleoperation



Apply F_d

Force Control makes F_c track F_d

System Setup

Control of a Mobile...

Teleoperation

Force Control

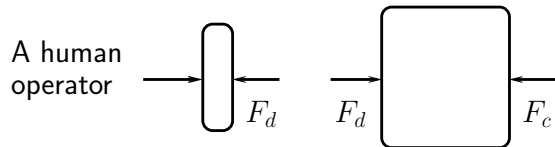
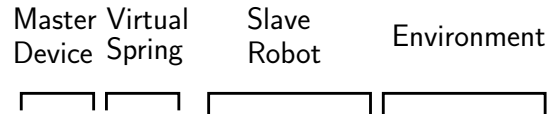
Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...

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Apply F_d

Force Control makes F_c track F_d

The human operator feels F_d .

$$F_c \approx F_d$$

System Setup

Control of a Mobile...

Teleoperation

Force Control

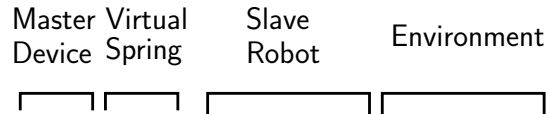
Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...

3. Teleoperation



A human operator

K_{vir}

Damping

K_s

Apply F_d

Force Control makes F_c track F_d

The human operator feels F_d .

$$F_c \approx F_d$$

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

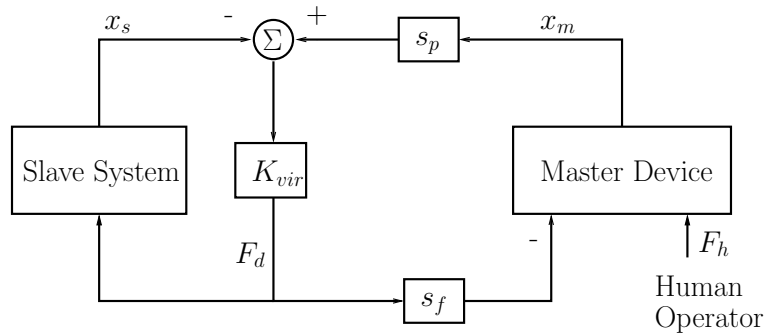
Experimental Results

Conclusion

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Block Diagram



- x_m, x_s Master and slave position
 s_p, s_f Scaling for position and force
 K_{vir} Virtual spring constant
 F_d Desired contact force for both master and slave



4. Force Control

With the equation of motion for each direction in the operational space coordinate,

$$\dot{v}_f = F_f^*$$

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...



4. Force Control

With the equation of motion for each direction in the operational space coordinate,

$$\dot{\vartheta}_f = F_f^*$$

and a spring model

$$\dot{F}_c = K_s \vartheta_f,$$

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...



4. Force Control

With the equation of motion for each direction in the operational space coordinate,

$$\dot{\vartheta}_f = F_f^*$$

and a spring model

$$\dot{F}_c = K_s \vartheta_f,$$

The system transfer function can be derived as

$$G(s) = \frac{K_s e^{-sT_d}}{s(s + K_2)}.$$

T_d system input delay

K_2 additional damping

System Setup

Control of a Mobile...

Teleoperation

Force Control

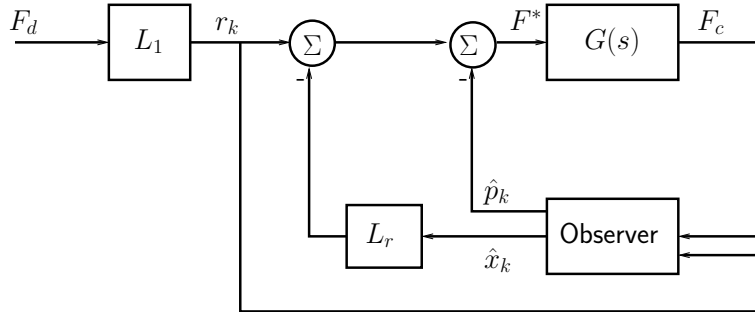
Stiffness Estimation

Experimental Results

Conclusion

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Block Diagram



- F_c Contact force at the end-effector
 F_d Desired contact force
 F^* Command input
 \hat{x}_k State estimate
 \hat{p}_k Input error estimate
 r_k, L_1 Reference input, and a scaling factor
 L_k Full state feed-back gain
 $G(s)$ System transfer function from F^* to F_c

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

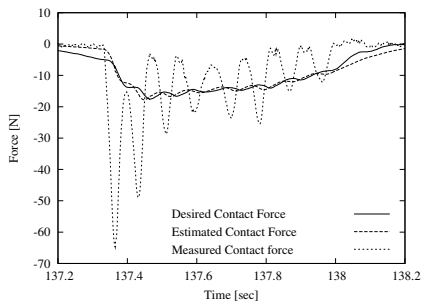
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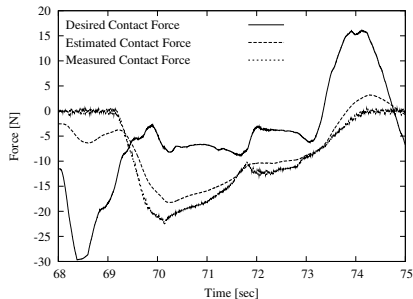


5. Stiffness Estimation

The results of force control without adaptation



$\hat{K}_s = 100 \text{ N/m}$
 K_s changes from
free space to 3000 N/m .



$\hat{K}_s = 3000 \text{ N/m}$
 K_s changes from
free space to 300 N/m .



Adaptation Law

Two Ideas from experiments: $\hat{K}_s^i = \hat{K}_{s,1}^{f,i} + \hat{K}_{s,2}^{f,i}$.

1. Under/Over-estimated K_s shows Different characteristics among the desired, measured, and estimated contact force.

$$\hat{K}_{s,1}^i = \hat{K}_{s,1}^{i-1} + \Delta \hat{K}_{s,1}^i,$$

where

$$\begin{aligned} \Delta \hat{K}_{s,1}^i &= k_1 |F_m - F_e| \sigma_d \left(c, \frac{|F_m - F_e|}{|F_e| + a_1} - b_1 \right) \\ &\quad - k_2 |F_d - F_e| \sigma_d \left(c, \frac{|F_d - F_e|}{|F_e| + a_2} - b_2 \right), \\ \sigma_d(c, x) &= \frac{1}{1 + e^{-cx}}. \end{aligned}$$

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...



Adaptation Law

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2. System stiffness, K_s , increases with the applied contact force.

$$\hat{K}_{s,2} = K_{min} + k_3 \sigma_d(c_0, |F_m| - F_0).$$



6. Experimental Results

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

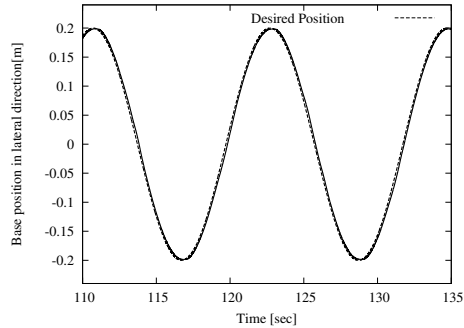
Experimental Results

Conclusion

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- Position Scale from Haptic Device to PUMA : 2.0
- Force Scale from PUMA to Haptic Device : 0.1
- Time Delay in communication : about 26 ms in one direction

Moving base teleoperation: Base Motion



Base motion in the lateral direction (i.e. along the table)
The amplitude is 20 cm and the period is 12 seconds.

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

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Moving base teleoperation: force response



System Setup

Control of a Mobile...

Teleoperation

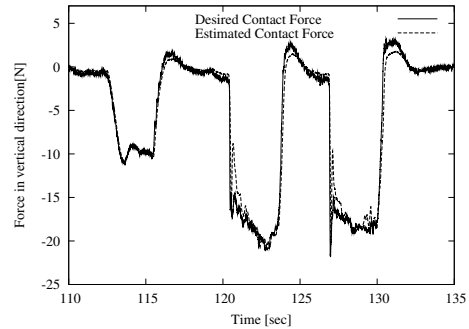
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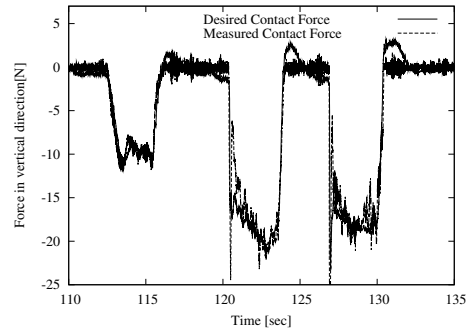
Experimental Results

Conclusion

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Desired and Estimated Contact Force



Desired and Measured Contact Force

Moving base teleoperation: \hat{K}_s and position tracking



System Setup

Control of a Mobile...

Teleoperation

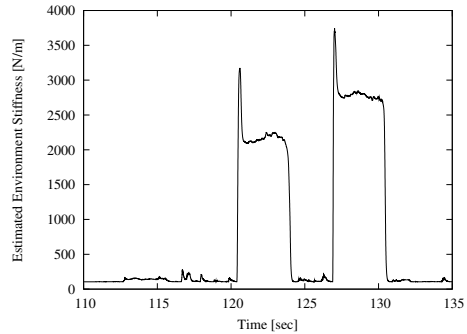
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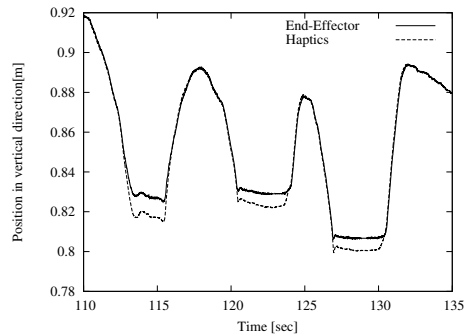
Experimental Results

Conclusion

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Estimated Environment Stiffness



End-effector Tracking Haptic Device Position

Moving base teleoperation: force comparison



System Setup

Control of a Mobile...

Teleoperation

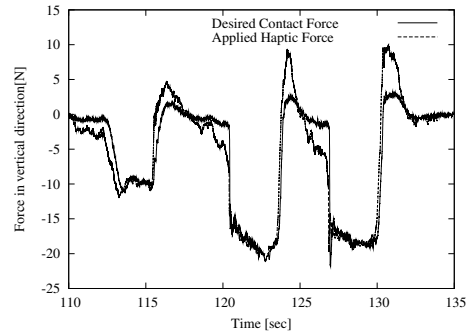
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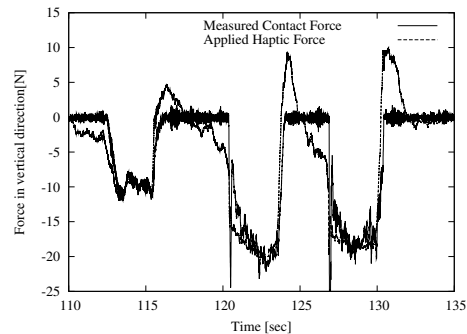
Experimental Results

Conclusion

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Desired Contact Force and Applied Haptic Force to User



Measured Contact Force and Applied Haptic Force to User



7. Conclusion

- Simple teleoperation scheme using an adaptive force control
- Robust force control using AOB(i.e. a modified Kalman estimator)
- Fast On-line stiffness adaptation
- Decoupled control strategy for a mobile manipulator.

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

Juliet Setting a Dinner...



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Future Work

- More systematic algorithm for stiffness adaptation
- Better user interface for redundant DOF of a mobile manipulator

System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

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8. Juliet Setting a Dinner Table



System Setup

Control of a Mobile...

Teleoperation

Force Control

Stiffness Estimation

Experimental Results

Conclusion

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