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Integrated Planning And Execution: Elastic Strips

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ABSTRACT

Real-time replanning is a prerequisite for motion execution in unpredictably changing environments. This paper presents a framework that allows real-time replanning in high-dimensional configuration spaces. Initially, a planning operation generates a path. The path is augmented by a set of paths homotopic to it. This set is represented implicitly by a volume of free space in the workspace. Effectively, this corresponds to delaying part of the planning operation until motion execution. During execution, reactive control algorithms select a valid path from the set of homotopic paths, using proximity to the environment as a simple and effective heuristic and thereby significantly pruning the search in the configuration space. Experimental results are presented to validate the real-time performance of this framework in high-dimensional configuration spaces.

KEYWORDS: real-time path modification, real-time replanning, motion execution, free space representation, collision avoidance

INTRODUCTION

Algorithms to generate robot motion have historically been divided into motion planning algorithms [12] and control algorithms [7]. While this distinction is vague and some algorithms cannot be exclusively attributed to either of these categories [6, 13], it is based on several fundamental properties of those methods. Motion planning algorithms are considered to generate a path that respects *global* motion constraints, whereas control algorithms only use *local* information to determine a motion command. Furthermore, motion planning algorithms compute the path *prior* to the motion execution, whereas control algorithms are determining motion commands based on feedback *during* motion execution. In addition, planning methods are generally *complete* or resolution complete, while control algorithms only optimize a local objective function and may therefore globally cause suboptimal behavior. This also holds for reactive methods, such as the potential field approach that exhibits *local minima* [9]. Generally, motion planning methods are of *high computational complexity*, whereas the computations for most control algorithms can be performed *many times per second*.

In unpredictably changing environments the applicability of motion planning algorithms is limited. Moving obstacles can invalidate a previously generated motion by obstructing the computed path. Should such a situation occur, a planning operation is computationally too complex to recompute a new path in real time, while continuously executing the motion. Control algorithms, on the other hand, can react to sudden changes in the environment, but might fail to achieve the desired goal configuration. This paper presents the latest results on the elastic strip framework [2, 3] that integrates planning and control algorithms into a motion generation approach, which allows real-time replanning in high-dimensional configuration spaces.

INTEGRATION OF PLANNING AND CONTROL

The computational complexity of motion planning methods is mostly determined by the cost of computing the free space. This can be attributed to two properties: Firstly, the search space has to be explored *globally*, and secondly, the size of the search space grows exponentially with the dimensionality of the configuration space. Attempts to render motion planning algorithms more efficient have taken these two properties as starting points.

The most efficient planning algorithms for high-dimensional configuration spaces avoid the computation of an explicitly free space representation. The free space is computed and represented implicitly, by applying sampling techniques to the configuration space [8]. This does not eliminate the dependency of the computational complexity on the dimensionality of the configuration space. The required number of samples to accurately represent the free space depends on the clutteredness of the configuration space, which generally increases with its dimensionality. Furthermore, these algorithms still have to explore the entire configuration space.

In an attempt to reduce the computational complexity of planning algorithms, methods were devised that use heuristics to locally explore the configuration space until a path is found [1, 5]. Those heuristics take advantage of information about the workspace to guide the local search in configuration space. The search relies on iterative or recursive methods to compute the boundary of free space around a particular configuration. For these methods the amount of computation will increase with the number of degrees of freedom of the robot because the extent of the free space region must be explored along every dimension of the configuration space.

The framework presented in this paper is applicable to replanning and therefore addresses a narrower problem than the approaches mentioned above. Motion planning methods reduce the complexity of motion planning by representing configuration space obstacles implicitly and by using workspace information to guide the exploration of configuration space. The elastic strip framework presented in the next section goes one step further: it delays the exploration of the configuration space until execution. During execution this exploration can be performed very efficiently using reactive control algorithms.

The underlying idea is to represent a set of homotopic paths by the workspace volume a robot would sweep out along them. This can be done without considering the kinematic properties of the robot, i.e. without exploring the configuration space. The prerequisite is the existence of a valid path, called candidate path. Assume a planner has generated such a candidate path and it lies entirely in free space. The free space around the candidate path must contain the volume swept by the robot along paths homotopic to the candidate path itself. Those paths are represented implicitly by an approximation of the free space around the candidate path, rather than computing them explicitly. During execution this set of homotopic paths can be searched very efficiently for an alternate valid path, should the candidate path be invalidated by changes in the environment.

Using such a representation, planning and control can be tightly integrated: The path generated by a motion planner is transformed into a more general representation by augmenting every path with an implicit representation of paths homotopic to it. Control algorithms can then be used during execution to efficiently search that space to find a valid path, should the original one become invalid due to changes in the environment. This is the underlying principle of the elastic strip framework described below.

ELASTIC STRIPS

The elastic strip framework allows real-time replanning by integrating planning and control. This integration relies on two important components: a simple representation of sets of homotopic paths and an efficient method of selecting a valid path from this set. Those components will be described in this section.

Sets of Homotopic Paths

An elastic strip represents the free space around an existing path using a set of overlapping spheres of workspace. Using only one distance computation, the free space around a point *p* in the workspace can be computed. Such a sphere of free space is called *bubble* [13]; it contains all points *q* that are close to *p* than the closest obstacle and is defined as $B(p) = \{q \mid p - q < r(p)\}$, where $r(p)$ computes the minimum distance from *p* to any obstacle.

A set of bubbles is used to describe the local free space around a configuration *q* of a robot *R*. This set is called *protective hull* P_q^R and is defined as $P_q^R = \bigcup_{p \in R} B(p)$. Not every point $p \in R$ needs to be covered by a bubble. A heuristic is used for selecting a small set of points yielding an accurate description of the free space around configuration *q*. An example of a protective hull around the Stanford Mobile Manipulator is shown in Figure 1.

Along the path or trajectory *U* a sequence of configurations $q_1, \cdots, q_n$ is chosen. This sequence is called an elastic strip S_T^R if the union of the protective hulls P_i^R of the configurations $q_i, 1 \le i \le n$ fulfills the condition $V_U^R \subseteq T_S^R = \bigcup_{1 \le i \le n} P_i^R$, where V_U^R is the workspace volume of robot *R* swept along the path *U*. The union T_S^R of protective hulls is called *elastic tunnel*. An example of an elastic tunnel is shown in Figure 2. Five configurations of the Stanford Mobile Manipulator along a given path are displayed. The overlapping bubbles of free space are shown as transparent spheres. The spherical obstacle in the middle is restricting the size of the bubbles. For clarity, other obstacles are not shown.

Figure 1. A protective Hull around the Stanford Mobile Manipulator

Relating the elastic strip framework to the discussion in the previous section, the initial path *U* corresponds to the candidate path, and the elastic tunnel implicitly represents a set of paths homotopic to it. Referring to Figure 2, it is easy to imagine how the volume swept by the robot along the path *U* is contained within the elastic tunnel *T*. It is also intuitive that the volume swept by the robot along a path *U'* that is homotopic to *U* and was obtained by a slight modification of *U*, would also be contained within the elastic tunnel. Therefore, an elastic tunnel can be viewed as a representation of a set of paths homotopic to the candidate path. As the elastic tunnel can be computed very efficiently with very few distance computations, this constitutes the first component necessary for the integration of planning and control described in the previous section.

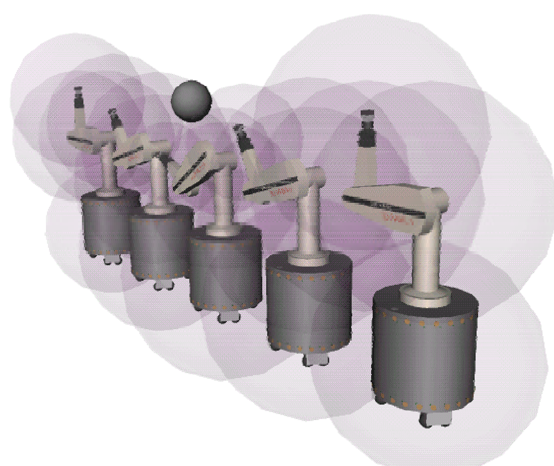

Figure 2. Elastic Tunnel in the presence of an obstacle.

Selection of a Path

Given a candidate path and an implicit representation of a set of paths homotopic to it, an algorithm is required to efficiently select a path from the elastic tunnel, if the candidate path is invalidated by changes in the environment. For this algorithm to be as efficient as possible, a simple potential field-based control algorithm is used. Rather than exploring the entire configuration space, it maps proximity information from the environment into the configuration space, using the kinematics of the manipulator.

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Figure 3. The structure of an elastic strip.

External and internal forces derived from artificial potential fields are used to modify the elastic strip's shape. The resulting behavior resembles that of a rubber band: Obstacles exert external forces and cause the elastic strip to deform to avoid collision. As obstacles recede, internal forces cause the elastic strip to assume a configuration that minimizes internal energy. The forces in workspace are mapped to joint displacements using a dynamic model of the manipulator. This replaces configuration space exploration with a directed search, guided by workspace forces indicating proximity to obstacles. This procedure is virtually independent of the number of degrees of freedom of the robot.

In case of redundant manipulators, dynamically consistent decoupling of task execution and null space motion [4, 10] can be applied. Motion in the null space of the task is used to avoid obstacles, shorten the trajectory, and achieve a desired posture, while continuously executing the task.

Updating the Sets

A roadmap captures the connectivity of the free space as a network of one-dimensional curves. As we are interested in dynamic environments that give rise to the need of replanning, it cannot be assumed that the roadmap will remain accurate. As a consequence for the replanning paradigm described in this paper, the sets of homotopic paths need to be updated in accordance with changes in free space connectivity. For example, an obstacle crossing a hallway from one side to another, introduces a second candidate path, or curve in the roadmap, as it moves away from the wall and can now be passed on either side. After contact with the opposing wall is made, the two candidate paths are merged again.

The motion of obstacles in the environment can cause substantial changes in the connectivity of the free space. Ultimately, the reinvocation of a motion planner is needed to guarantee completeness. In most practical environments, however, the motion of obstacles translates to small changes of overall free space connectivity. Since the goal is to avoid a costly motion planning operation, local planning methods or heuristics can be used to update the roadmap. This subsection presents two of those local replanning operations that are integrated with the elastic strip framework [2].

In populated environments, the most frequent type of change impacting the candidate path, is an obstacle crossing the path. As a result, it is deformed, as can be seen in the first image of Figure 4. By imposing constraints on the internal forces acting between two adjacent configurations along the elastic strip, the obstacle can be allowed to "pop through" the elastic strip, as shown in the top row of Figure 4. Internal forces then will reconnect the path, after the obstacle has passed. If internal forces cannot reconnect the path, a different local replanner or a global motion planner can be invoked [2].

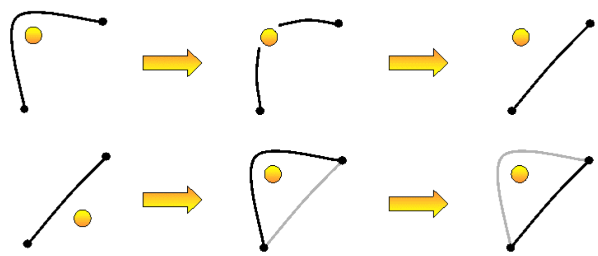

Figure 4. Examples of local replanning methods

Alternatively, the roadmap computed by the planner could always be maintained as a set of alternative routes. These routes can become invalid, if obstructed by obstacles. The obstacle will cause portions of the original roadmap to change. If the obstruction is removed, however, the path in the original roadmap can again become a valid candidate path. This is illustrated in Figure 4, where a moving obstacle causes a path to be deformed. Further obstacle motion unblocks the original candidate path, which now is valid again and represents the shortest path between the two points.

EXPERIMENTAL RESULTS

The elastic strip framework was tested in simulation and experimentally with various platforms [2]. Figure 5 shows two experiments with the Stanford Mobile Manipulator. The Stanford Mobile Manipulator is a nine degree-of-freedom robot, consisting of a holonomic base and a six degree-of-freedom PUMA 560. The first series of images in Figure 5 shows how four PA-10 robots move into the path of the Stanford Mobile Manipulator. The first image of this sequence shows the candidate path, as computed by the planner. The subsequent pictures show how a new path is selected in real-time, as the motion of obstacles invalidates the original path. The replanning operation in the nine-dimensional configuration space is performed about 10 times per second on a 400 MHz Pentium PC. For simpler examples replanning rates of up to 100 Hz were achieved. The path is smoothened during execution. The other sequence of images shows a similar experiment for two Stanford Mobile Manipulators.

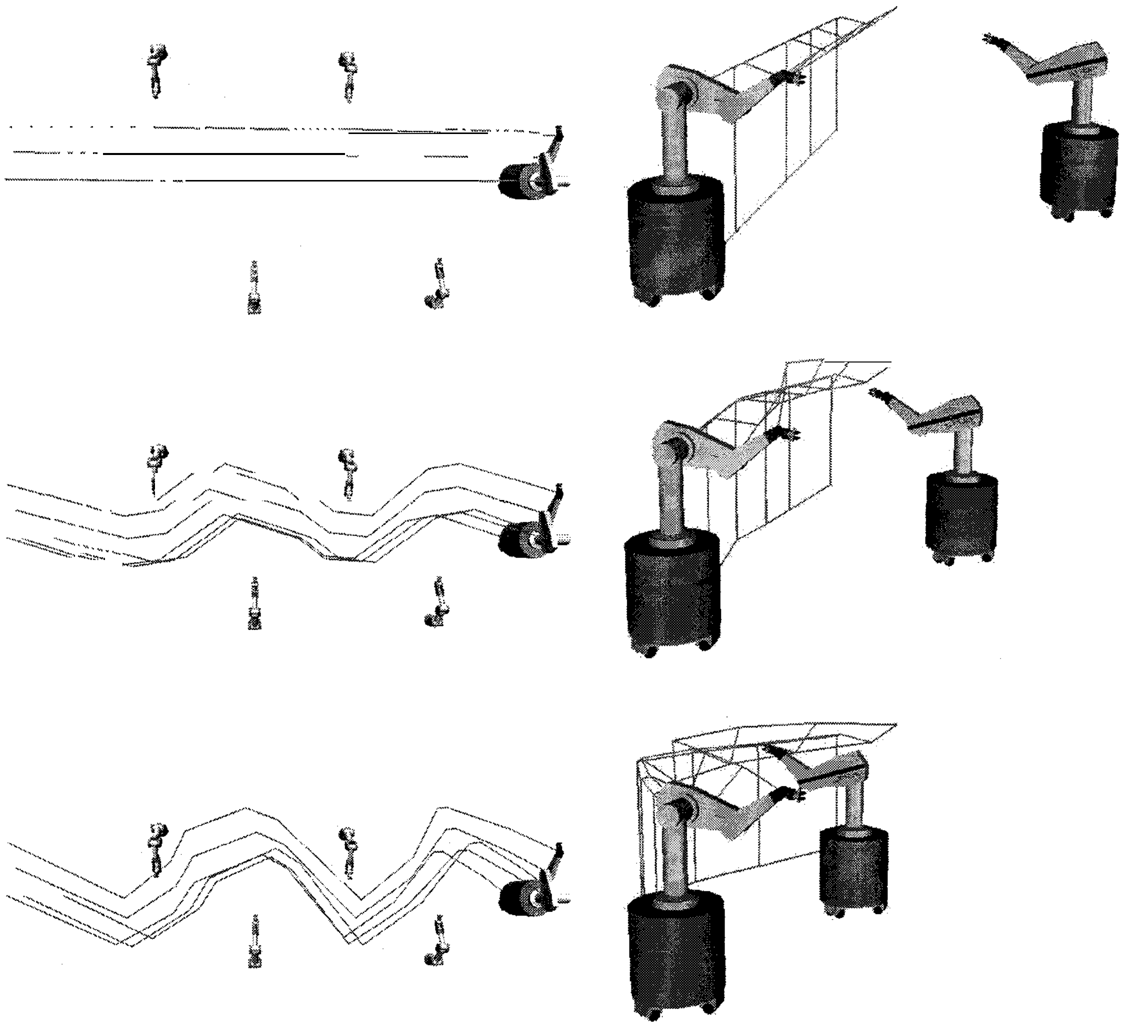

Figure 5. On the left: Four manipulator arms move into the path of the Stanford Mobile Manipulator; replanning using elastic strips is performed in real-time to maintain a valid path. The path is indicated by lines connecting points on consecutive configurations along the elastic strip. It is converted into a smooth trajectory during execution. On the right: A Stanford Mobile Manipulator moves into the path of another one. The path is updated in real-time to avoid a collision.

CONCLUSION

Conventionally, the link between planning and control is a path. To execute the path, it is first converted into a trajectory and then executed by control algorithms. Such a path can be represented as a set of via points, a parametric descriptions of joint positions as a function of time, or as a navigation function [1 1].

The elastic strip framework relies on the existence of a valid candidate path, previously obtained by a planner. Using the notion of elastic tunnel as an implicit representation of sets of homotopic paths as the connecting link, the elastic strip framework realizes a much tighter integration of planning and control than previous approaches. This generation until execution, rendering replanning significantly more efficient. Experiments have proven the elastic strip framework to be an effective and efficient way of performing replanning in real-time, even in high-dimensional configuration spaces.

The replanning operation performed by the elastic strip framework is incomplete and may result in suboptimal paths. It can be augmented with other replanning primitives that allow handling most practical situations. Ultimately, elastic strips cannot replace planning itself: if changes in the environment are substantial and the elastic strip framework cannot find a valid candidate path, the reinvocation of a complete planner becomes necessary.

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